p-values Had a Good Run: A Primer on the 'New Statistics'

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Part 7: Meta-Analysis

- Meta-Analysis
 - The statistical summarization of the effects from a set of studies investigating the same research question
 - However, the term 'meta-analysis' often also applies to the entire process of generating a research question, finding studies that investigate the research question, extracting the necessary info from the studies, and combining the results from the related studies

Systematic Review

- In some instances "systematic review" and "meta-analysis" are used interchangeably, whereas in other instances the term systematic review refers to the procedures used to collect the studies of interest (i.e., those to be combined), and meta-analysis refers to the statistical combination of the effects from these studies
 - Systematic Review
 - A review of studies addressing a research question that is conducted according to clearly stated methods

Some History from Psychology

- 1952: Hans Eysenck concluded that there were no favorable effects of psychotherapy, starting a raging debate
 - 20 years of evaluation research and hundreds of studies failed to resolve the debate
- 1978: To prove Eysenck wrong, Gene Glass statistically aggregated the findings of 375 psychotherapy outcome studies
 - Glass concluded that psychotherapy did indeed work
- Glass called his method "meta-analysis"

The Emergence of Meta-Analysis

- Ideas behind meta-analysis predate Glass' work by several decades
- Karl Pearson (1904)
 - Averaged correlations for studies of the effectiveness of inoculation for typhoid fever
- R. A. Fisher (1944)
 - We can combine the results of several studies to get an appreciation for the probability associated with the aggregated data
 - Dealt primarily with combining *p*-values
- The start of the idea of *cumulating probability* values, although not specifically focused on effect sizes

The Emergence of Meta-Analysis

- W. G. Cochran (1953)
 - Discussed a method for averaging means across independent studies
 - Cochran was responsible for much of the statistical foundation that modern meta-analysis is built upon
- Cochrane Collaboration
 - A group of researchers from around the world that conduct systematic reviews of health-care interventions and diagnostic tests and publishes them in the Cochrane Library
 - e.g., https://canada.cochrane.org/

The Logic of Meta-analysis

- Traditional methods of review focus on statistical significance testing
 - E.g., the effect was statistically significant in 4 out of 7 studies
 - However, we know that NHST is highly related to sample size
- Meta-analysis focuses on the *direction* and *magnitude* of the effects across studies, not statistical significance
 - Direction and magnitude are represented by the effect size

When Can You Do Meta-analysis?

- Studies are empirical, not theoretical
- Results are quantitative, not qualitative
- Studies examine the same research question
- Results can be quantified in a comparable statistical form
 - i.e., effect size

Research Questions Amenable to Meta-Analysis

- Central tendency research (e.g., means)
 - Pre-post contrasts
 - Group contrasts
 - Experimentally created groups
 - E.g., comparison of treatment and control groups
 - Naturally occurring groups
 - E.g., comparing executive functioning in bilingual and monolingual individuals
- Associations among variables
 - Correlations/Regression Coefficients
 - E.g., correlation between perfectionism and depression

Answerable/Unanswerable Research Questions

- Unanswerable Research Questions
 - What is the best strategy to prevent smoking in young people?
 - How do we cure diabetes?
- Answerable Research Questions
 - Are mass media interventions effective in preventing smoking in young people?
 - E.g., smoking rates in a community from pre-intervention to post-intervention
 - Combine pre-post mean differences
 - Is sugar intake related to glycemic levels in young children?
 - Combine correlations

Which Studies to Review?

- Should be as inclusive as possible
 - Need to find ALL studies
 - Published studies are easy to find ... unpublished studies are not
 - The inclusion of unpublished studies helps to minimize the effects of *publication bias*
- Apples and Oranges
 - A priori inclusion and exclusion criteria must be laid out
 - It is imperative that the studies being meta-analyzed address the same research question

Exploring Publication Bias

Funnel Plot

- A plot of the size of the effect of a study against the precision of a study
- Symmetrical funnel plots provide evidence of a lack of publication bias, where asymmetrical funnel plots highlight that publication bias might be present
 - E.g., if effects with low precision seem to all have larger effects then publication bias is likely

Funnel Plot



Symmetrical vs Asymmetrical Funnel Plot



А

В

Where To Find Studies

- Computerized bibliographic databases
 Google Scholar, Psycinfo, Medline, ERIC
- Authors working in the research domain
 - Personal websites (e.g., Researchgate, OSF), psyarchiv
- Conference programs
- Dissertations
- Reference lists from relevant articles

What Information Should be Collected?

- Think about these long and hard before starting data collection ... it sucks to have to go back and recollect data
 - Publication details
 - Or specific location details for unpublished studies
 - Study design
 - Population details (N, characteristics)
 - Intervention/Design details
 - Operational Definitions of Variables
 - Demographics and other potential moderators
 - Outcomes
 - E.g., Means, SDs, correlations, regression coefficients, variability of coefficients, sample sizes

Why Assess the Validity of Studies?

- Lower quality studies can have biased outcome results
 - E.g., Allocation to Treatment/Control
 - Inadequate allocation concealment (e.g., investigators playing a role in allocation) exaggerated treatment effects by about 35% (Moher, 1998; Schulz, 1995)
 - E.g., Blinding
 - Lack of blinding of subjects exaggerated treatment effects by 17% (Schulz, 1995), or increased the effect size by about a half a SD (Hróbjartsson et al., 2014)

Where Can Bias be Introduced into Studies?

- Selection bias
- Allocation bias
- Confounds
- Blinding
- Data collection methods
- Withdrawals and drop-outs
- Statistical analysis
- Intervention integrity
- Summary: Lots of ways that bias can be introduced into research

Assessing the Validity of a Study

- The most common way to assess and report study quality has been using a composite, numerical scoring instrument
 - Many different quality assessment instruments are available, with most designed for randomized clinical trials
- ▶ E.g., Jadad Score for Experiments (0-3)
 - Was the study described as randomized?
 - Was the study described as double blind?
 - Was there a description of withdrawals and dropouts?

Methodological Quality Dilemma

- Include or exclude low quality studies?
 - The findings of all studies are potentially in error (methodological quality is a continuum, not a dichotomy)
 - Being too restrictive may limit ability to generalize
 - Being too inclusive may weaken the confidence that can be placed in the findings
 - Methodological quality is often subjective
 - You must strike a balance that is appropriate to your research question
- When including low quality studies you can weight effects by study quality or explore study quality as a moderator

Level of Replication

- Replications can range from "conceptual" replications to "pure" or "direct" replications
 - Direct replications are the repetition of an experimental procedure to as exact a degree as possible, whereas a conceptual replication is the use of different methods/procedures to repeat the test of a hypothesis
- You must be able to argue that the collection of studies you are meta-analyzing examine the same relationship
- The closer to pure replications your collection of studies, the easier it is to argue comparability of the effect from each study

Effect Size in Meta-Analysis

Effect size is the "dependent variable"

- It standardizes findings across studies such that they can be directly compared
- A standardized index must be comparable across studies, represent the magnitude and direction of the relationship of interest and be independent of sample size
 - e.g., standardized mean difference, correlation coefficient, odds-ratio

We already discussed effect sizes in detail

Forest Plot

- A visual representation of the effect sizes (and confidence intervals for the effect sizes) of the multiple studies included in a meta-analysis
 - All effects must be measured in the same metric, e.g., correlation
- The size of the effect size icons (e.g., squares) indicates the "weight" of the study to the combined effect
 - E.g., larger N studies have a higher weight
- The plot also shows the effect size (and confidence interval for the effect size) of the combined effect across studies

Forest Plot Example - Odds Ratios



Fixed Effects vs Random Effects

- There are two popular models available for conducting a meta-analysis
 - In other words, two models available for arriving at a "combined" measure of effect size
 - Fixed Effects Model
 - Assumes that all the studies investigated the same population, and therefore estimate the same population effect size
 - Highly questionable
 - Random Effects Model
 - Allows for the possibility that the studies investigated somewhat different populations, and therefore estimate different population effect sizes

Fixed Effects vs Random Effects

- It is difficult to imagine a setting in which multiple studies conducted in different locations, with different samples, and with potentially different measures all are studying the same population (and thus after a single population effect size)
- The random effects model is more realistic and provides a basis for understanding the heterogeneity of effect sizes
 - Further, the models give the same answer if there is only a single population so it is hard to find a reason for a researcher to prefer a fixed effects model

Fixed Effects Meta-Analysis

For a set of S effect size measures (γ)

$$\circ \widehat{\mathbf{Y}}_F = \frac{\sum_{i=1}^S w_i \widehat{\mathbf{Y}}_i}{\sum_{i=i}^S w_i}$$

•
$$w_i = \frac{1}{s^2(\widehat{\gamma}_i)}$$

• $s^2(\widehat{\gamma}_F) = \frac{1}{\sum_{i=i}^S w_i}$

Random Effects Meta-Analysis

For a set of S effect size measures (γ)

$$\widehat{\mathbf{Y}}_{R} = \frac{\sum_{i=1}^{S} w_{i} \widehat{\mathbf{Y}}_{i}}{\sum_{i=i}^{S} w_{i}}$$

$$w_{i} = \frac{1}{s^{2}(\widehat{\mathbf{Y}}_{i}) + \tau^{2}}$$

$$\tau^{2} = \frac{Q - (S - 1)}{\sum_{i=i}^{S} w_{i} - \frac{\sum_{i=i}^{S} w_{i}^{2}}{\sum_{i=i}^{S} w_{i}}} \text{ for } \mathbf{Q} > \mathbf{S} - 1$$

$$Q = \sum_{i=i}^{S} w_{i} (\widehat{\mathbf{Y}}_{i} - \widehat{\mathbf{Y}}_{F})^{2}$$

Heterogeneity of Effect Sizes

- A simple goodness-of-fit test can be used to test for excessive heterogeneity
 - Q ~ $\chi^2_{df=S-1}$
 - We reject the null that there is no population heterogeneity if $Q \ge \chi^2_{\alpha,df=S-1}$
- The problem with this approach is that the test has low-power when S is small

Heterogeneity of Effect Sizes

A better approach to quantifying heterogeneity is to use an effect size measure

$$I^2 = \frac{Q - S + 1}{Q}$$

I² ranges from 0 to 1, with larger values indicating more heterogeneity

Summary: Steps of a Systematic Review/Meta-Analysis

- Specific your research question/effect of interest
- Find studies that investigate the effect of interest
- Extract all necessary information from the studies
- Assess the validity of the studies and determine inclusion/exclusion/weighting
- Estimate the combined effect size and CI for the effect size
- Explore moderators of the variability in effect sizes
- Interpret the findings

Strengths of Meta-Analysis

- Imposes strict procedures on the process of summing up research findings
- Represents findings in a more sophisticated manner than conventional reviews
- Capable of finding relationships across studies that are obscured in other approaches or without amalgamation
- Capable of detecting moderators of effects
- Can handle a large numbers of studies, which would be difficult in a qualitative review

Weaknesses of Meta-Analysis

- Requires a lot of effort!
- Mechanical aspects don't lend themselves to capturing more qualitative distinctions between studies
- "Apples and oranges"
 - Comparability of studies is often in the "eye of the beholder"
- Most meta-analyses include "blemished" studies
- Selection bias possesses continual threat
 - E.g., Null finding studies are hard to find